

$$y = \log_a x \Leftrightarrow a^y = x \quad (a, x > 0, y \in \mathbb{R}) \quad \log_a m^n = n \log_a m$$

$$\log_a 1 = 0$$

$$\log_a m = \log_b m \cdot \log_a b$$

$$\log_a a = 1$$

$$\log_a m = \frac{\log_b m}{\log_b a}$$

$$\log_a mn = \log_a m + \log_a n$$

$$\log_a b = \frac{1}{\log_b a}$$

$$\log_a \frac{m}{n} = \log_a m - \log_a n$$

$$\log_a x = \frac{\ln x}{\ln a} = (\log_a e) \ln x$$